Opacity: Insurance and Fragility

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Transparency

• A cause of recent financial and economic crisis

"Financial firms sometimes found it quite difficult to fully assess their own net derivatives exposures.... The associated uncertainties helped fuel losses of confidence that contributed importantly to the liquidity problems" (Ben Bernanke, testimony, 2010)

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Transparency

• A cause of recent financial and economic crisis

"Financial firms sometimes found it quite difficult to fully assess their own net derivatives exposures.... The associated uncertainties helped fuel losses of confidence that contributed importantly to the liquidity problems" (Ben Bernanke, testimony, 2010)

• Widespread calls for transparency in the banking system

"To promote the financial stability of the United States by improving accountability and transparency in the financial system" (Dodd-Frank Act)

 requirements for ABS issues to provide more information about the underlying asset pool (Regulation AB II)

Opacity

• Counterargument:

- the banking system has been historically and purposefully opaque
- this opacity enables banks to issue information insensitive liabilities:
 - \star when the backing asset is difficult to assess,
 - \star the value of bank liabilities do not vary over some period of time

by Gorton (2013 NBER), Holmström (2015 BIS), Dang et al. (2017 AER)

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Debates on transparency vs. opacity

This paper

• Q. Should the banking system be transparent or opaque?

- many dimensions to consider
- This paper addresses the question
 - from the view of financial stability
 - ► opacity ⇒ difficulty of assessing asset qualities
 - prime example: Asset Backed Commercial Paper conduits
- Show: uncertainty created by opacity:
 - provides insurance against risky assets (Hirshleifer, 1971 AER)

- raises incentive to run on the bank
- Describe: when the degree of opacity should be regulated

What drives a run?

- There are some works on this topic
 - focus: more information may trigger a bank run
 - show: transparency worsens financial stability (Bouvard et al. (2015 JF), Faria-e Castro et al. (2017 ReStud)...etc)

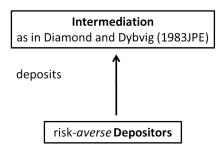
My contribution:

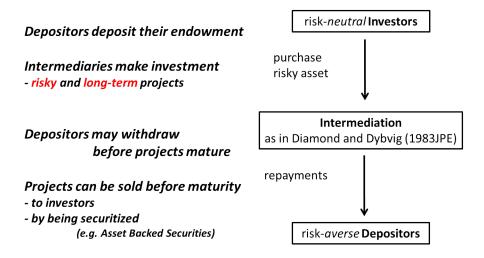
- focus: opacity itself makes depositors more likely to panic
- show: opacity worsens financial stability
- study trade-off between enhanced risk-sharing and higher fragility
- explain when opacity should be regulated

Literature Review

Depositors deposit their endowment

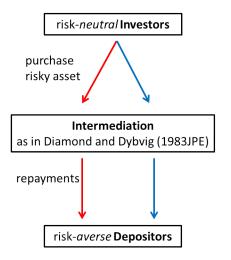
Intermediaries make investment - risky and long-term projects





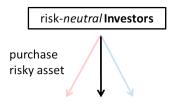
Once asset qualities are known...

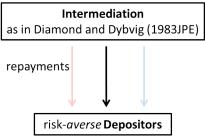
- Price will depend on realized qualities - Depositors face risk



While asset qualities are <u>un</u>known...

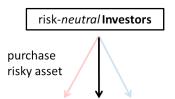
- Price depends on <u>expected</u> qualities - Investors face risk





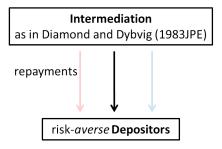
While asset qualities are <u>unknown</u>...

Price depends on <u>expected</u> qualities
 Investors face risk



Opacity transfers risk:

- Insurance for depositors
- ... but only in the short-term: - Influences withdrawal decisions



Overview

1 Model: the Environment

- 2 Equilibria
- Optimal opacity
- Onobservable choice of opacity

Depositors

My model is based on Diamond and Dybvig (1983 JPE)

- $t = \{0, 1, 2\}$
- Continuum of mass 1 depositors
 - endowed 1 unit of goods in t = 0 and consume in t = 1, 2
 - liquidity shock: π depositors need to consume in t = 1 (*impatience*)

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Technology and Market

Augmented to have Allen and Gale (1998 JF) technology and market

- A risky project
 - ▶ 1 invested in t = 0 yields $\left\{ \begin{array}{c} R_b \\ R_{\pi} \end{array} \right\}$ with prob $\left\{ \begin{array}{c} n_g \\ n_b \end{array} \right\}$ in t = 2

- indexed by $j \in \{b,g\}$, where $n_g + n_b = 1$
- realized in period 1

Technology and Market

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- A risky project
 - ▶ 1 invested in t = 0 yields $\left\{ \begin{array}{c} R_b \\ R_{\sigma} \end{array} \right\}$ with prob $\left\{ \begin{array}{c} n_g \\ n_b \end{array} \right\}$ in t = 2
 - indexed by $j \in \{b,g\}$, where $n_g + n_b = 1$
 - realized in period 1
- A competitive asset market
 - A large number of risk-neutral investors
 - ★ large endowment in period 1
 - given expected return $\mathbb{E}R$, investors drive asset price to $p = \rho \mathbb{E}R$

Intermediation

- **Bank**: collects deposits in t = 0
 - allows depositors to choose when to withdraw
 - t = 1: payments made sequentially on first-come-first-serve basis
 - the order of withdrawals is random and unknown
 - t = 2: remaining payments made by dividing matured projects evenly
 - operated to maximize expected utility of depositors

Sequential service

Intermediation

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Sequential service

- *Opacity* of asset $\theta \in [0, \pi]$
 - asset return revealed after θ withdrawals have been made
 - ***** before θ ; nobody knows R_i
 - * after θ ; everybody know R_j
 - ='time required to investigate R_i '

Runs and Sunspot

- *Runs* occur when patient depositors withdraw in t = 1
- Withdrawals may be conditioned on sunspot $s \in S = [0, 1]$
 - allows for the possibility that a bank run may occur in equilibrium (Cooper and Ross, 1998 JME, Peck and Shell, 2003 JPE)
 - ▶ bank does not observe $s \Rightarrow$ is initially uncertain if a run is underway in period 1

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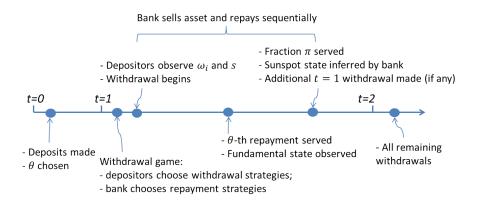
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 - bank does not observe s ⇒ is initially uncertain if a run is underway in period 1
- At π withdrawals, the bank reacts
 - ▶ at this point, the run stops (Ennis and Keister, 2009 AER).
 - bank's reaction restores confidence in the bank
 - No commitment:
 - * Diamond-Dybvig: commitment prevents a self-fulfilling run
 - * Here: prohibited to use this time-inconsistent policy
 - bank allocates remaining consumption efficiently

Timeline



Withdrawal game

• Given θ , the bank and depositors play a simultaneous-move game:

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- depositor i maximizes her expected utility
- the bank maximizes the expected utility of depositors

Withdrawal game

- Given θ , the bank and depositors play a simultaneous-move game:
 - depositor i maximizes her expected utility
 - the bank maximizes the expected utility of depositors
- My interest: the following *cutoff strategy profile* of depositors $\hat{y}_i(\omega_i, s; q) = \begin{cases} \omega_i \\ 0 \end{cases}$ if $s \begin{cases} \geq \\ < \end{cases} q$ for some $q \in [0, 1], \forall i$.
 - introducing the likelihood of runs (Peck and Shell, 2003 JPE)

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Intuition: a bank run occurs with probability q

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 - introducing the likelihood of runs (Peck and Shell, 2003 JPE)
 - Intuition: a bank run occurs with probability q
- **Repayment** depends on \hat{y}_i and her position in the line
 - before θ , funded by selling assets at a pooling price $p_u = \mathbb{E}p_j$
 - after θ in period 1, funded by selling assets at p_j
 - in period 2, funded by realized return of matured assets R_j

Overview

Model: the Environment

2 Equilibria

Optimal opacity

Onobservable choice of opacity

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Equilibrium bank runs

• Is there an equilibrium in which depositors follow this cutoff strategy?

- answer depends on q
- When a run is more likely $(q \uparrow)$:
 - ▶ banks are more conservative: give less to early withdrawers ⇒ giving less incentive for patient depositors to run

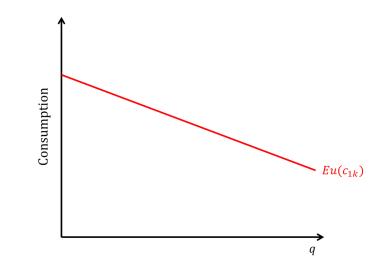
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- Define $\bar{q} = \max$ value of q such that $\hat{y}(q)$ is an equilibrium strategy

- that is, maximum equilibrium probability of a bank run
- I use \bar{q} as the measure of financial fragility

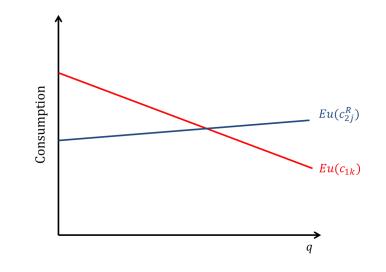
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- Define $\bar{q} = \max$ value of q such that $\hat{y}(q)$ is an equilibrium strategy
 - that is, maximum equilibrium probability of a bank run
- I use \bar{q} as the measure of financial fragility
 - **Q.** How does the level of opacity (θ) affect financial fragility (\bar{q}) ?
 - \Rightarrow need to compare expected payoffs of patient depositors.

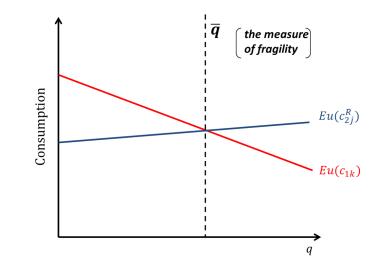


Result: expected payoffs in period 1 are monotonically decreasing in q

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Result: expected payoffs in period 2 are monotonically increasing in q



Result: $\mathbb{E}u(c_{2j}^R) \leq \mathbb{E}u(c_{1k})$ when $q \leq \bar{q}$ \Rightarrow the cutoff strategy profile is a part of equilibrium

Impact of opacity

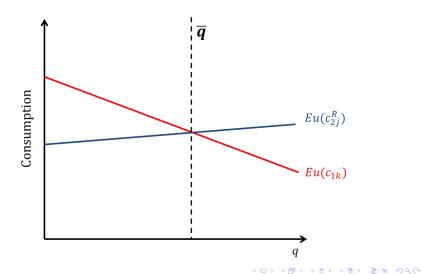
• Recall: expected payoffs depend on $\boldsymbol{\theta}$

Q. How does an increase in θ affect equilibria?

Impact of opacity

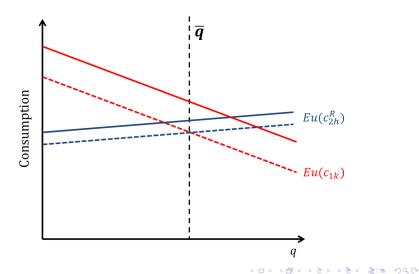
 \bullet Recall: expected payoffs depend on θ

Q. How does an increase in θ affect equilibria?



An increase in θ

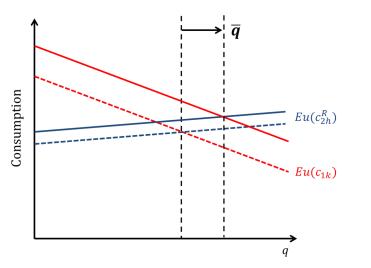
- raises chance of receiving insurance in t = 1: $\mathbb{E}u(c_{1k}) \uparrow\uparrow$
- has indirect effects through (c_{1k}, c_{2j}^R) : $\mathbb{E}u(c_{2j}^R)$ \uparrow



Proposition

• \bar{q} is increasing in θ

 \Rightarrow Opacity increases fragility



Opacity increases fragility

• This result is novel in the literature

- Literature: information causes bank runs
- Here: no information causes self-fulfilling bank runs

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- Opacity
 - provides insurance by transferring risks
 - increases financial fragility
 - \Rightarrow **Q**. What is the optimal degree of opacity?

Overview

- Model: the Environment
- 2 Equilibria
- Optimal opacity
- Onobservable choice of opacity

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Pessimistic views

- Recall $U(c^*, y^*; \theta)$ depends on θ .
 - \blacktriangleright multiple equilibria associated with each choice of θ

Pessimistic views

• Recall $U(c^*, y^*; \theta)$ depends on θ .

- \blacktriangleright multiple equilibria associated with each choice of θ
- Focus on the worst-case scenario:

$$max_{\theta}min_{q\in\mathcal{Q}(\theta)} U(c^*, \hat{y}(q); \theta)$$

- Intuition: minimizing losses in the worst case over $q \in \mathcal{Q}(\theta)$.
- the worst case $\Rightarrow \bar{q}(\theta)$ (:: $U(c^*, \hat{y}(q); \theta)$ is decreasing in q)

Pessimistic views

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- Intuition: minimizing losses in the worst case over $q \in \mathcal{Q}(\theta)$.
- the worst case $\Rightarrow \overline{q}(\theta)$ (:: $U(c^*, \hat{y}(q); \theta)$ is decreasing in q)

• Anticipating the worst equilibrium outcomes, the bank solves $max_{\theta \in [0,\pi]} U(c^*, \hat{\gamma}(\bar{q}(\theta)); \theta)$

trade-off: Hirshleifer effect versus Fragility effect

Result: For some parameter values, $\theta^* < \pi$.

Numerical example

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Numerical example

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The optimal opacity becomes larger when:

• the discount rate of investors ρ increases.

Result: For some parameter values, $\theta^* < \pi$.

Numerical example

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The optimal opacity becomes larger when:

- the discount rate of investors ρ increases.
- assets are riskier
 - the gap of returns between fundamental states (R_g/R_b) increases,
 - the fundamental state is more uncertain (when *n* is closer to $\frac{1}{2}$).

Overview

- Model: the Environment
- 2 Equilibria
- Determining optimal opacity

O Unobservable choice of opacity

I have assumed that θ is observable. ⇒ Q. How does the bank behave if θ is not observable?

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Unobservable choice of opacity

• In the previous analysis:

depositors could directly observe their bank's choice of $\boldsymbol{\theta}$

• Now: Suppose instead this information is difficult to observe

- Intuition: depositors may find it difficult to know which of assets takes a longer time to investigate
- In the model,
 - depositors can still make inferences and understand bank's incentives

- expectations will be correct in equilbrium
- but bank cannot credibly reveal its choice

Regulating opacity

• Result: The bank's dominant strategy is the highest possible opacity.

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- > a larger opacity can still provide insurance to more depositors
- depositors cannot observe the level of opacity

Regulating opacity

• Result: The bank's dominant strategy is the highest possible opacity.

- ▶ a larger opacity can still provide insurance to more depositors
- depositors cannot observe the level of opacity
- Welfare comparison
 - the bank may become more opaque θ^{**} = π ≥ θ^{*}
 ⇒ equilibrium outcomes may be worse for depositors

Regulating opacity

• Result: The bank's dominant strategy is the highest possible opacity.

- a larger opacity can still provide insurance to more depositors
- depositors cannot observe the level of opacity
- Welfare comparison
 - the bank may become more opaque θ^{**} = π ≥ θ^{*}
 ⇒ equilibrium outcomes may be worse for depositors
- Regulating opacity
 - ▶ imposing an observable upper bound on θ so that $\theta \in [0, \theta^*]$

- the conditional dominant strategy of bank is now θ^*
- \blacktriangleright the outcome is the same as when θ is observable
- Example: limiting asset classes of investment

Conclusion

• I have presented a model of financial intermediation where:

- opacity determines time required to investigate asset quality
- repayment and withdrawal behavior are chosen given the opacity
- bank chooses the opacity anticipating equilibrium outcomes
- I show that opacity increases fragility
- In choosing opacity, a bank faces trade-off between:
 - providing insurance by keeping asset return unknown
 - ► increasing fragility by raising incentives to run ⇒ optimal level of opacity is often interior
- Bank becomes maximally opaque if its choice is unobservable
 - In this case, regulating opacity may improve welfare

Thank you

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Literature

- Effect of opacity on risk-sharing Hirshleifer (1971AER), Kaplan (2006ET), Dang et al. (2017AER)
- Effect of opacity on financial stability
 - positive effects: Parlatorre (2015WP), Chen and Hasan (2006JFI, 2008JMCB), Faria-e Castro et al. (2016ReStud)
 - mixed effects: Bouvard et al. (2015JF), Ahnert and Nelson (2016WP)
- Effect of opacity on bank's risk-taking Hyytinen and Takalo (2002RoF), Moreno and Takalo (2016JMCB), Jungherr (2016WP)

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Literature

- Bank anticipates the possibility of runs
 Peck and Shell (2003 JPE), Cooper and Ross (1998 JME)
- Bank trades assets in financial markets Jacklin (1987), Allen and Gale (1998 JF), Allen and Gale (2000 JPE)
- Bank is prohibited from using time-inconsistent policy (i.e. suspension)
 Ennis and Keister (2009 AER), Ennis and Keister (2010 JME)

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Sequential services

- Agents are isolated from each others
- Repayments are made immediately as each agent arrive
- Order of withdrawal opportunities is random
- Depositors do not know their position in the order (Peck and Shell, 2003 JPE)
- Each agent can contact the bank either in period 1 or period 2



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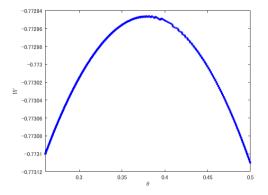
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Numerical example:



given $(\gamma, \pi, n, R_g, R_b, \rho) = (2, 0.5, 0.5, 2, 1, 0.9).$

Modified banking problem

Given $\hat{y}(q)$, the bank chooses $(\theta, c_1, \{c_{1j}, c_{1j}^N, c_{2j}^N, c_{2j}^R\}_{j=b,g})$ to maximize

$$\max_{\substack{[\theta,c_1,\{c_{1j},c_{1j}^N,c_{2j}^R\}_{j=b,g}]}} \frac{\theta u(c_1) + \sum_j n_j \left[(\pi - \theta) u(c_{1j}) + (1 - q)(1 - \pi) u(c_{2j}^N) + q(1 - \pi) [\pi u(c_{1j}^R) + (1 - \pi) u(c_{2j}^R)] \right]$$

subject to

$$(1-\pi)\frac{c_{2j}^{N}}{R_{j}} = 1-\theta\frac{c_{1}}{p_{u}} - (\pi-\theta)\frac{c_{1j}}{p_{j}},$$

$$\pi(1-\pi)\frac{c_{1j}^{R}}{p_{j}} + (1-\pi)^{2}\frac{c_{2j}^{R}}{R_{j}} = 1-\theta\frac{c_{1}}{p_{u}} - (\pi-\theta)\frac{c_{1j}}{p_{j}}, \forall j.$$

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