Title: Grothendieck fibrations, or When aesthetics drives mathematics

Grothendieck introduced fibrations to describe sheaves of categories. In its simplest form a fibration would represent a family of categories indexed by a category. But that presentation is quite ugly. We shall try to describe how Grothendieck turned that into not just a beautiful definition, but into a fundamental concept for today's mathematics.